



# Formal Modeling for UML/MARTE Concurrency Resources

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# Motivation



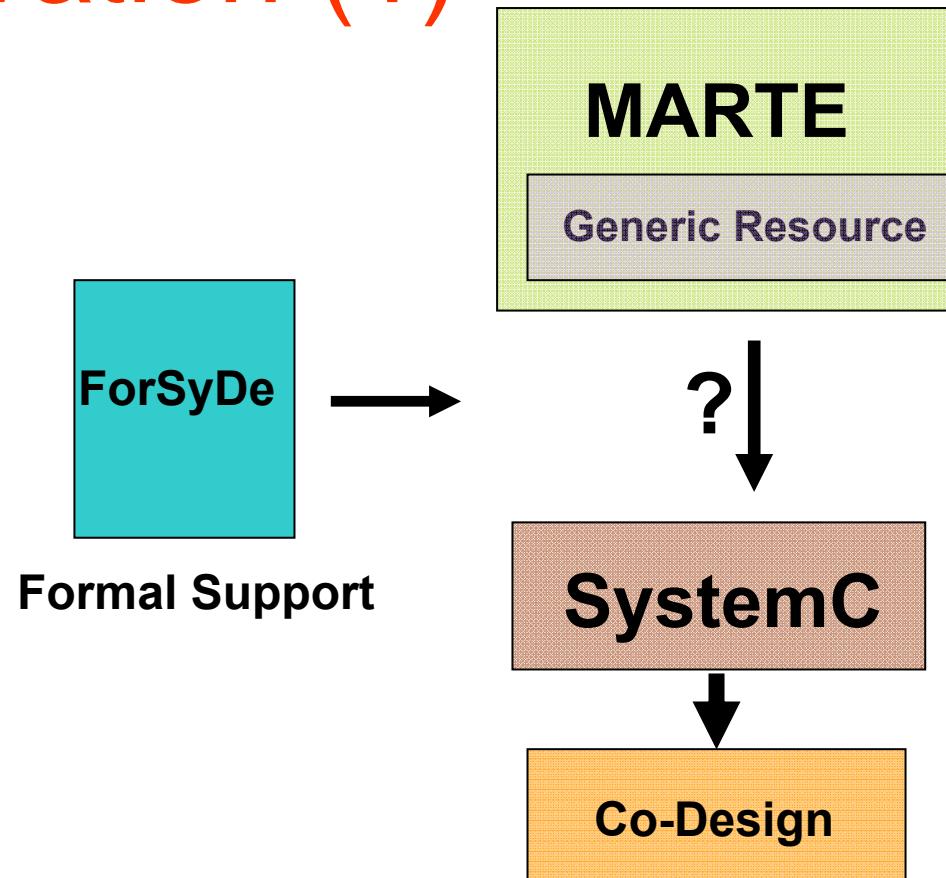
# Motivation (1)

**MARTE** provides  
semantics to UML

Select a subset of MARTE

Relate UML/MARTE to SystemC

SystemC enables a  
link to Co-Design



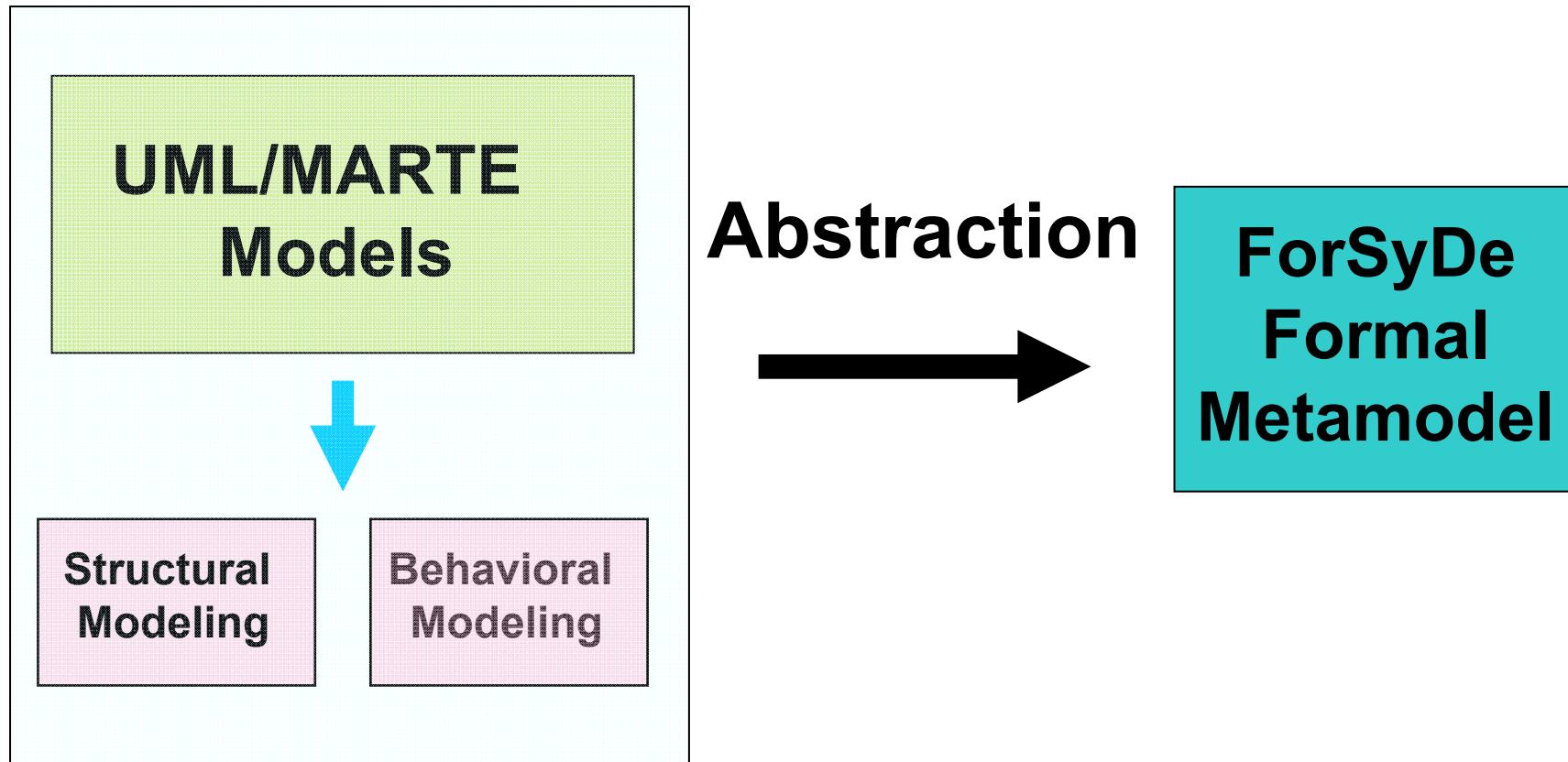


# Motivation (2)

- **Massive Concurrency**
  - Data Dependencies
  - Relations
- **Characteristic of the interactions**
  - Formal Semantics
  - Univocal Description
- **Models of Computation & Communication (MoCCs)**
  - Behaviors Semantics Heterogeneity



# Contribution



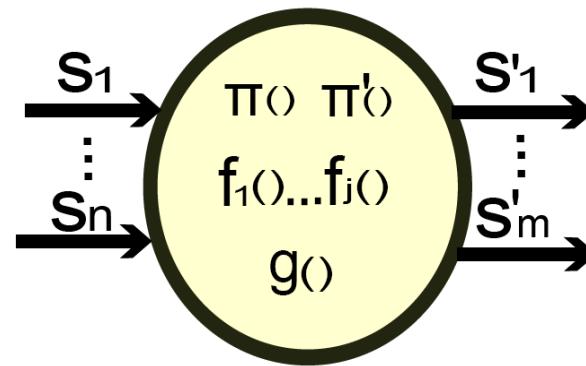


# Formal System Design

- ForSyDe formal metamodel
  - *Process*
  - *Signals*
    - Separation Communication-Computation
  - *MoCC generic characteristics*
    - Untimed MoCCs
    - Synchronous MoCCs
    - Timed MoCCs



# Process ForSyDe



$$p(s_1 \dots s_n) = s'_1 \dots s'_m$$

$\pi$  partition function  $S_n$

$\pi'$  partition function  $S'_m$

$g()$  next-state function

$f_1()$ ... $f_j()$  output functions



# Formal Notation

The partitions functions:

$$\pi(v_n, s_n) = \langle a_n(z) \rangle \quad \pi'(v'_m, s'_m) = \langle a'_m(z) \rangle$$

where  $a_n(z)$  is a subsignal of  $S_n$

The function  $v_n$  gives the size of  $a_n(z)$ :

$$v_n(z) = \gamma(\omega_q) \quad v'_m(z) = \text{length}(a'_m(z))$$

$$v_n(0) = \text{length}(a_n(0)); \quad v_n(1) = \text{length}(a_n(1))\dots$$

The outputs are calculated:

$$f_\alpha((a_1 \dots a_n), \omega_q) = (a'_1 \dots a'_m)$$

And the next internal state:

$$g((a_1 \dots a_n), \omega_q) = \omega_{q+1}$$

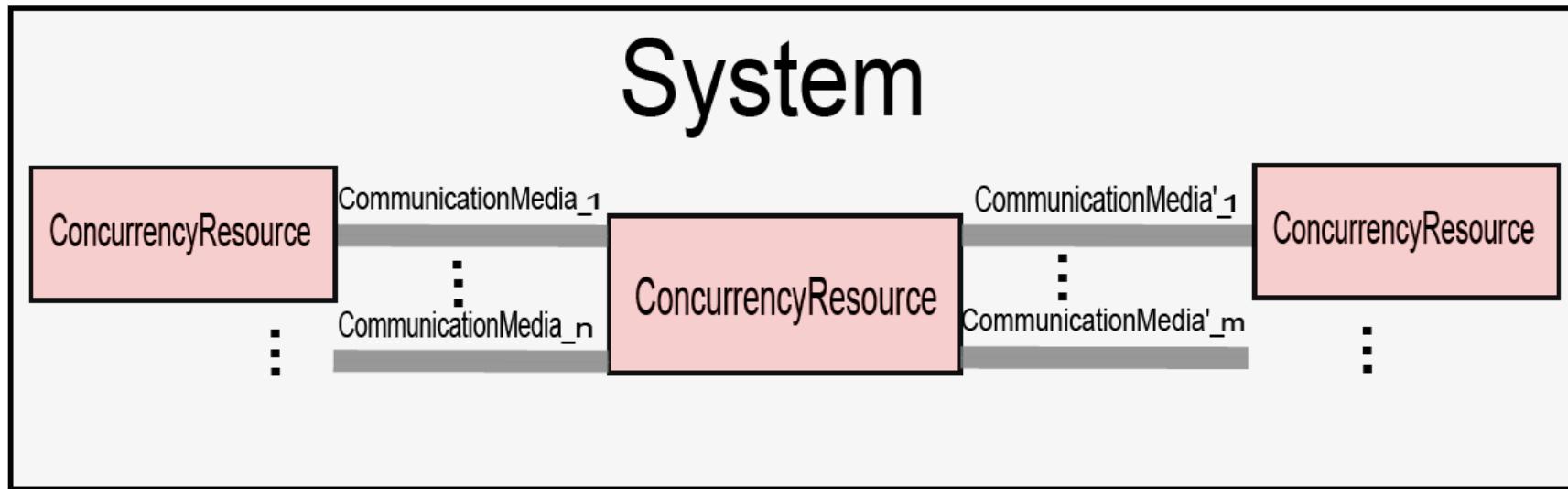


# UML/MARTE

## Methodology



# Structural Modelling



**<<ConcurrencyResource>>: models the concurrent computation**

**<<CommunicationMedia>>: models the communication**



# Communication Abstraction

ForSyDe  
Signals

↑ abstraction

<<CommunicationMedia>>

No insert any change in the data sequence:

- No data losses or injections
- No data values changes



# Behavioral Modeling

- Concurrent element described by a Finite State Machine
  - UML Finite State Machines
    - Explicit States
    - Modeling behavior State denoted by the label *do* by an UML Activity Diagram
  - UML Activity Diagram
    - Implicit States as a sequence of actions

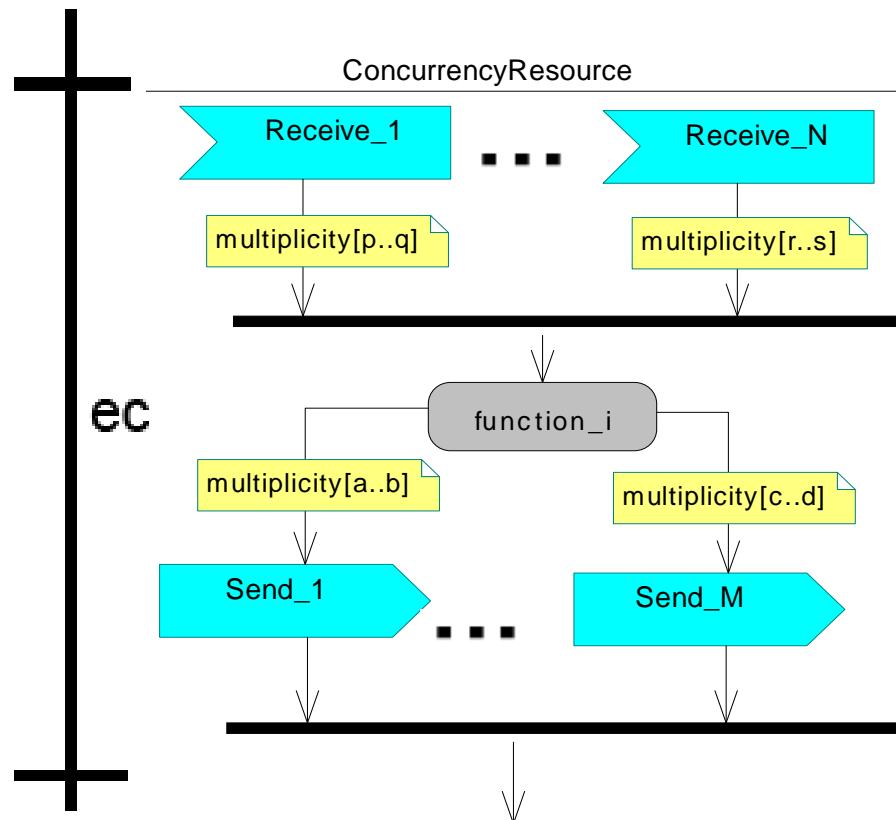


# Activity Diagram

- In each state
  - A set of inputs are received
  - These inputs are computed
  - The computation results are generated
  - The concurrency resource calculates its new internal state



# Activity Diagram(2)



**AcceptEventActions**

$$\omega_j = \begin{cases} P_j \\ D_j \end{cases}$$

**SendObjectAction**



# Activity Diagram(3)

- *AcceptEventAction*
  - Call to a specific method with a specific data-receiving behavior
  - A new datum is available
- *SendObjectAction*
  - Call to a specific method with a specific data-sending behavior
  - A new datum is generated



# Computation Abstraction

- The data received;  $a_1 \dots a_N$  ForSyDe subsignals
- The data send;  $a'_1 \dots a'_N$  ForSyDe subsignals
- The *function\_i* action;  $f_\alpha$  ForSyDe function
- The Concurrency Resource State:
  - $P_j$ ; segments of the behavioural modelling between two waiting states
  - $D_j$ ; internal values that characterizes the state
- $\{P_j, D_j\}; \omega_j$  ForSyDe state
- The function  $g()$  calculates the new  $\{P_{j+1}, D_{j+1}\}$



# Computation Abstraction(2)

- The multiplicity values are abstracted as:

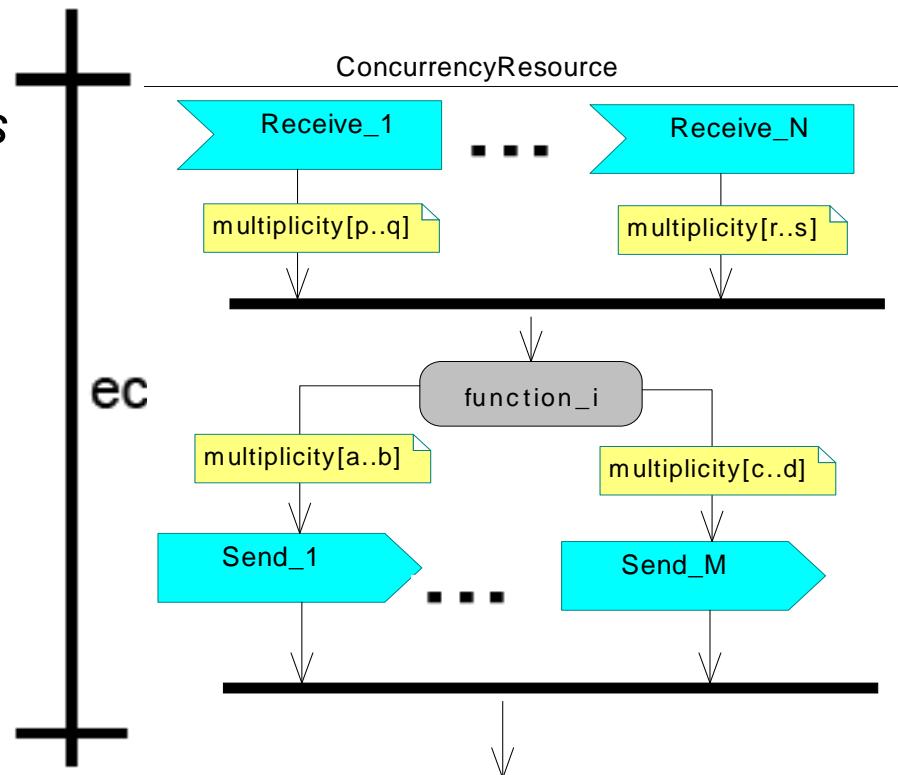
$$\nu_1(z) = \gamma(\omega_j) = \begin{cases} p \\ \dots \\ q \end{cases}$$
$$\nu_n(z) = \gamma(\omega_j) = \begin{cases} r \\ \dots \\ s \end{cases}$$

$$\text{length}(f_j(a_1 \dots a_N), \omega_j) = \begin{cases} \nu'_1(z) = \text{length}(a'_1) \begin{cases} a \\ \dots \\ b \end{cases} \\ \dots \\ \nu'_M(z) = \text{length}(a'_M) \begin{cases} c \\ \dots \\ d \end{cases} \end{cases}$$



# Computation Abstraction(3)

- The advance of time is a totally ordered set of *evaluation cycles* (**ec**).
- In each **ec** “a process consumes inputs, computes its new internal state, and emits outputs”.
- The interpretation of a **ec** depends on the time domain capture in the models.

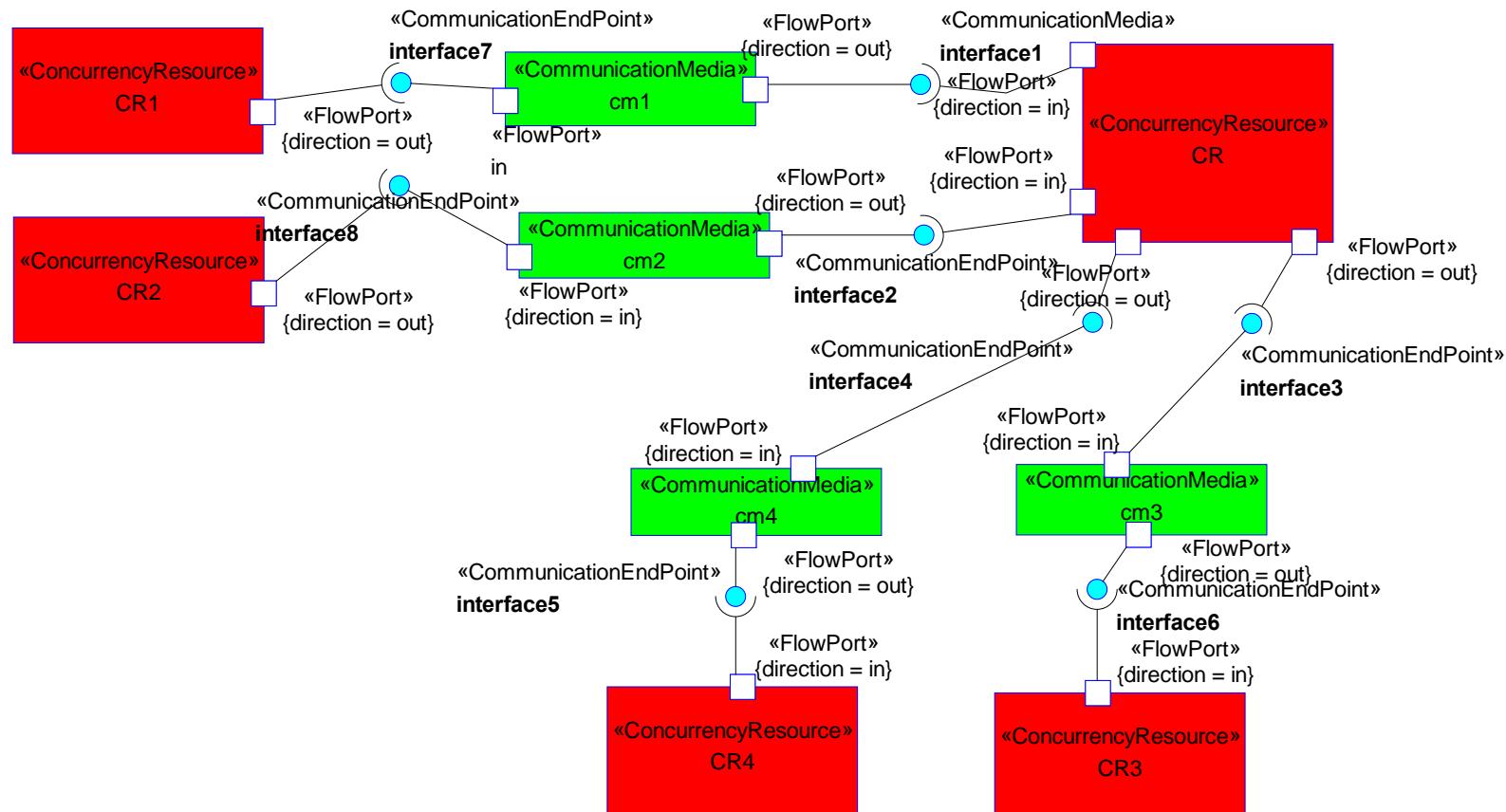




# Example

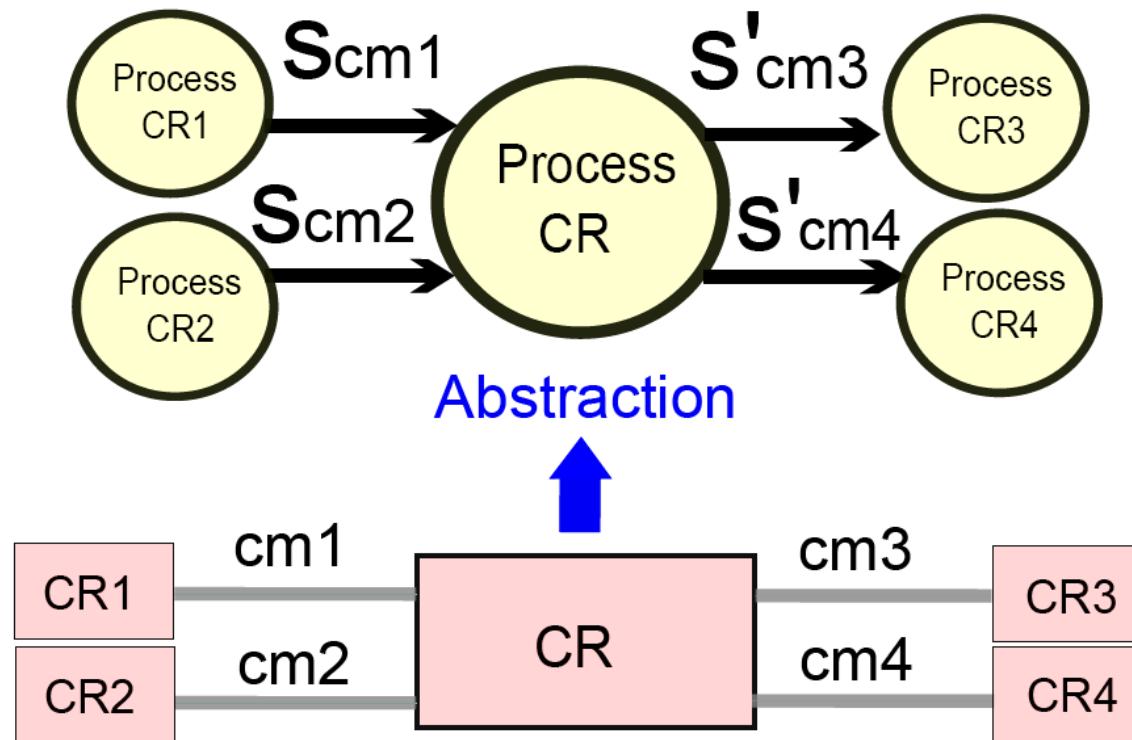


# Example(1)



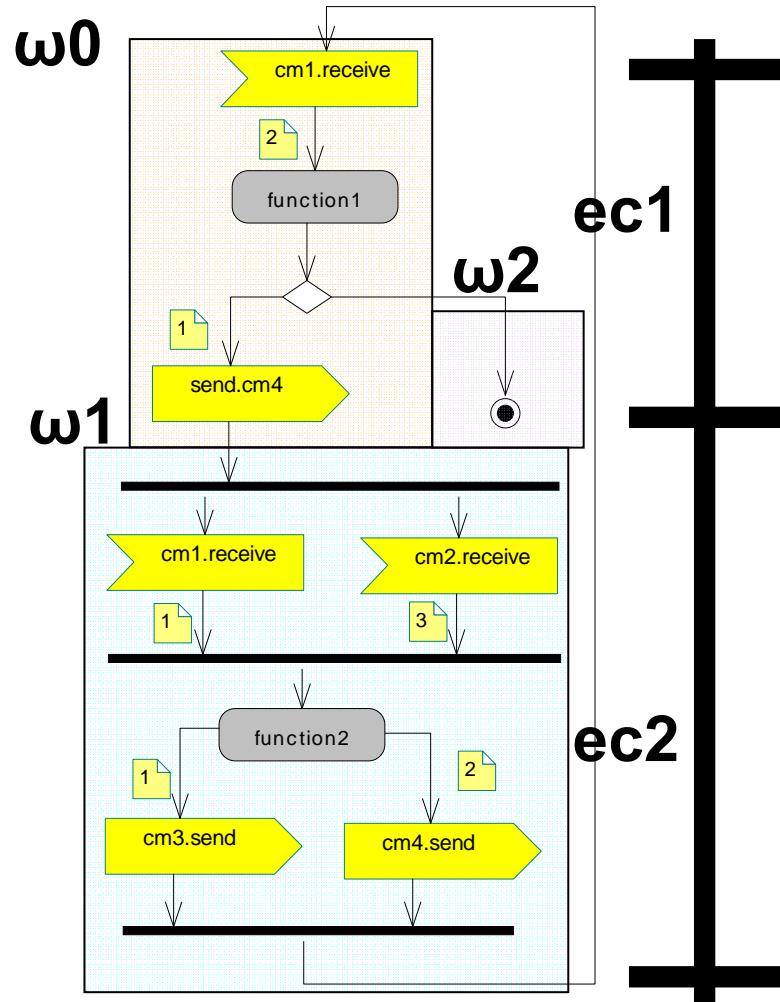


# Example(2)





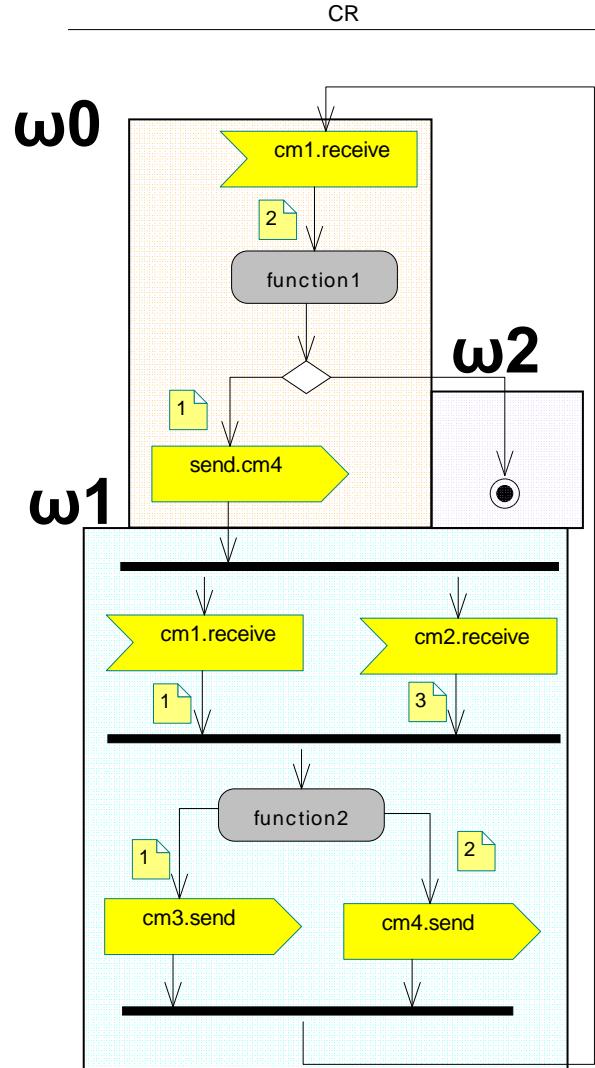
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data inputs       $a_{cm1}(z), a_{cm2}(z)$   
 data outputs       $a'_{cm3}(z), a'_{cm4}(z)$

$$g(\omega_0, a_{cm1}) = \begin{cases} \omega_1 \\ \omega_2 \end{cases}$$

$$g(\omega_1, (a_{cm1}, a_{cm2})) = \omega_0$$



# Example(4)

In the state  $\omega_0$ :

$$\nu_{a_{cm1}}(0) = \gamma(\omega_0) = 2$$

$$\begin{aligned} \nu_{a_{cm4}}(0) &= \text{length(function1}(a_{cm1}(0), \omega_0)) = \\ &= \text{length}(a'_{cm4}(0)) = 1 \end{aligned}$$

In the state  $\omega_1$ :

$$\nu_{a_{cm1}}(1) = \gamma(\omega_1) = 1$$

$$\nu_{a_{cm2}}(0) = \gamma(\omega_1) = 3$$

$$\begin{aligned} \nu_{a_{cm3}}(0) &= \text{length(function2}((a_{cm1}(1), a_{cm2}(0)), \omega_1)) = \\ &= \text{length}(a'_{cm3}(0)) = 1 \end{aligned}$$

$$\begin{aligned} \nu_{a_{cm4}}(1) &= \text{length(function2}((a_{cm1}(1), a_{cm2}(0)), \omega_1)) = \\ &= \text{length}(a'_{cm4}(1)) = 2 \end{aligned}$$



# Conclusions

- The need of a formalism to UML/MARTE models that supports the generation of executable specifications (SystemC)
- ForSyDe can provides this formal support